

Introduction: The Universal Language of Formulas

Mathematics is often described as the universal language of the universe, and at the heart of this language lies a vast collection of formulas. A **list of all formulas in mathematics** is more than just a reference sheet; it represents the distilled wisdom of centuries of human thought, from ancient Babylonian tablet calculations to cutting-edge quantum theory. Formulas serve as compact expressions of relationships, enabling us to solve problems, predict outcomes, and understand the patterns that govern everything from a falling apple to the orbit of a distant galaxy.

For students, educators, and professionals alike, having a structured **list of all formulas in mathematics** at their fingertips can transform the daunting task of problem-solving into a manageable, systematic process. This article provides a comprehensive, organized walkthrough of the essential formulas across every major branch of mathematics, presented in a clean, easy-to-navigate format. Whether you are preparing for an exam, refreshing your knowledge, or simply curious about the building blocks of mathematical logic, this guide will serve as a valuable reference.

Understanding that math is cumulative, we will begin with foundational arithmetic and algebra before moving through geometry, trigonometry, calculus, statistics, and discrete mathematics. By the end, you will have a complete **list of all formulas in mathematics** that highlights the interconnectedness of these diverse fields.

Foundational Arithmetic and Number Theory Formulas

Before diving into complex variables and derivatives, it is essential to master the basic operations and properties of numbers. These formulas form the bedrock upon which all higher mathematics is built. A comprehensive **list of all formulas in mathematics** must always begin here, as these rules govern how numbers interact in every subsequent calculation.

Basic Operations and Properties

The commutative, associative, and distributive properties are the three pillars of arithmetic. They dictate that the order of addition or multiplication does not affect the result, but this does not hold for subtraction or division. The distributive property links addition and multiplication: **a(b + c) = ab + ac**. These properties are not just rules; they are the logical framework that ensures consistency across all mathematical systems.

Exponents and Radicals

Exponents provide a shorthand for repeated multiplication. The key formulas include:

- Product of Powers:** $a^m \times a^n = a^{m+n}$
- Quotient of Powers:** $a^m \div a^n = a^{m-n}$
- Power of a Power:** $(a^m)^n = a^{m \times n}$
- Zero Exponent:** $a^0 = 1$ (where $a \neq 0$)
- Negative Exponent:** $a^{-n} = 1 / a^n$
- Fractional Exponents:** $a^{m/n} = \sqrt[n]{a^m}$

Radicals, or roots, are the inverse of exponents. The square root and cube root are the most common, with the general formula being $\sqrt[n]{a} = a^{1/n}$. Understanding these relationships is crucial when working with any **list of all formulas in mathematics** involving growth, decay, or geometric scaling.

Factors and Multiples

Prime factorization, greatest common divisor (GCD), and least common multiple (LCM) are essential for simplifying fractions and solving ratio problems. The Euclidean algorithm provides an efficient method for finding the GCD of two numbers: **GCD(a, b) = GCD(b, a mod b)**. Repeating this process until the remainder is zero yields the greatest common divisor.

Algebra: The Language of Variables

Algebra introduces the concept of variables, allowing us to generalize arithmetic operations. No **list of all formulas in mathematics** would be complete without the vast array of algebraic identities and equation-solving techniques that form the toolkit for virtually every other branch of mathematics.

Basic Algebraic Identities

These are the building blocks for expanding and factoring expressions:

- Square of a Sum:** $(a + b)^2 = a^2 + 2ab + b^2$
- Square of a Difference:** $(a - b)^2 = a^2 - 2ab + b^2$
- Difference of Squares:** $a^2 - b^2 = (a + b)(a - b)$
- Sum of Cubes:** $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
- Difference of Cubes:** $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- Cube of a Sum:** $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$
- Cube of a Difference:** $(a - b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$

Quadratic Equations

The quadratic formula is arguably one of the most famous entries in any **list of all formulas in mathematics**. For a quadratic equation in the form $ax^2 + bx + c = 0$, the solutions are given by:

x = [-b ± √(b² - 4ac)] / (2a)

The discriminant, **Δ = b² - 4ac**, determines the nature of the roots: if $\Delta > 0$, there are two distinct real roots; if $\Delta = 0$, there is one repeated real root; if $\Delta < 0$, there are two complex conjugate roots. The sum of the roots is $-b/a$, and the product is c/a , relationships known as Vieta's formulas.

Systems of Linear Equations

For two variables, the solution to the system $ax + by = e$ and $cx + dy = f$ can be found using Cramer's Rule, which employs determinants. The formulas for x and y are:

- x = (ed - bf) / (ad - bc)**
- y = (af - ec) / (ad - bc)**

The denominator, $ad - bc$, is the determinant of the coefficient matrix. If this determinant is zero, the system either has no solution or infinitely many solutions.

Logarithms and Exponentials

Logarithms are the inverses of exponential functions. The fundamental properties include:

- Product Rule:** $\log_b(xy) = \log_bx + \log_by$
- Quotient Rule:** $\log_b(x/y) = \log_bx - \log_by$
- Power Rule:** $\log_b(x^n) = n \log_bx$
- Change of Base:** $\log_bx = \log_ax / \log_ab$

Geometry: The Mathematics of Space

Geometry deals with shapes, sizes, and the properties of space. From ancient Greek mathematicians to modern architects, geometric formulas have been essential for measuring and constructing the physical world. A reliable **list of all formulas in mathematics** must include the fundamental relationships that describe lines, angles, surfaces, and volumes.

Two-Dimensional Shapes

These formulas govern the perimeter and area of common planar figures:

- Circle:** Area = πr^2 , Circumference = $2\pi r$
- Triangle:** Area = $(1/2) \times \text{base} \times \text{height}$
- Rectangle:** Area = length $\times$ width, Perimeter = $2(\text{length} + \text{width})$
- Square:** Area = side², Perimeter = $4 \times \text{side}$
- Parallelogram:** Area = base $\times$ height
- Trapezoid:** Area = $(1/2) \times (\text{base}_1 + \text{base}_2) \times \text{height}$

Three-Dimensional Shapes

Volume and surface area formulas are critical for applications in physics, engineering, and design:

- Sphere:** Volume = $(4/3)\pi r^3$, Surface Area = $4\pi r^2$
- Cube:** Volume = side³, Surface Area = $6 \times \text{side}^2$
- Rectangular Prism:** Volume = l $\times$ w $\times$ h, Surface Area = $2(lw + lh + wh)$
- Cylinder:** Volume = πr^2h , Surface Area = $2\pi rh + 2\pi r^2$
- Cone:** Volume = $(1/3)\pi r^2h$, Lateral Surface Area = $\pi r\sqrt{r^2 + h^2}$
- Pyramid:** Volume = $(1/3) \times \text{base area} \times \text{height}$

Coordinate Geometry

Also known as analytic geometry, this branch connects algebra and geometry using a coordinate system. The distance between two points (x_1, y_1) and (x_2, y_2) is given by **d = √[(x₂ - x₁)² + (y₂ - y₁)²]**. The midpoint formula is **M = ((x₁ + x₂)/2, (y₁ + y₂)/2)**. The slope of a line, m, is calculated as **m = (y₂ - y₁) / (x₂ - x₁)**.

Trigonometry: The Mathematics of Angles

Trigonometry studies the relationships between the sides and angles of triangles. It is indispensable in fields such as astronomy, navigation, engineering, and physics. Any thorough **list of all formulas in mathematics** must dedicate significant attention to trigonometric identities and functions.

Basic Trigonometric Functions

For a right triangle with an angle θ :

- Sine:** $\sin \theta = \text{opposite} / \text{hypotenuse}$
- Cosine:** $\cos \theta = \text{adjacent} / \text{hypotenuse}$
- Tangent:** $\tan \theta = \text{opposite} / \text{adjacent}$
- Cosecant:**